

General relativistic hydrodynamics of non-convex stellar collapse: gravitational waves



Nicolas Sanchis-Gual
Departamento de
Astronomía y Astrofísica

José M. Ibáñez, NSG, José A. Font, Miguel A. Aloy, Susana Serna, Antonio Marquina. In preparation.

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Introduction

An open issue in relativistic astrophysics is the knowledge of the equation of state (EOS) describing the thermodynamical properties of high-density matter. Such extreme conditions are achieved in the cores of neutron stars.

With the recent detection of gravitational radiation, a significant new channel to collect complementary information and improve our understanding of the dense-matter EOS will soon be opened.

Its properties and the possible existence of exotic states may critically influence the stability and dynamics of these objects. The dense-matter EOS also plays a fundamental role in the evolution (on a hydrodynamical timescale) of scenarios of relativistic astrophysics such as core-collapse supernovae, short and long-duration progenitors of gamma-ray bursts, the cooling of protoneutron stars, the formation of stellar-mass black holes, or the merger of compact-binary systems.

From a theoretical point of view, the existence of such exotic states of matter in the dense-matter EOS also requires the analysis of the “convexity” of the EOS.

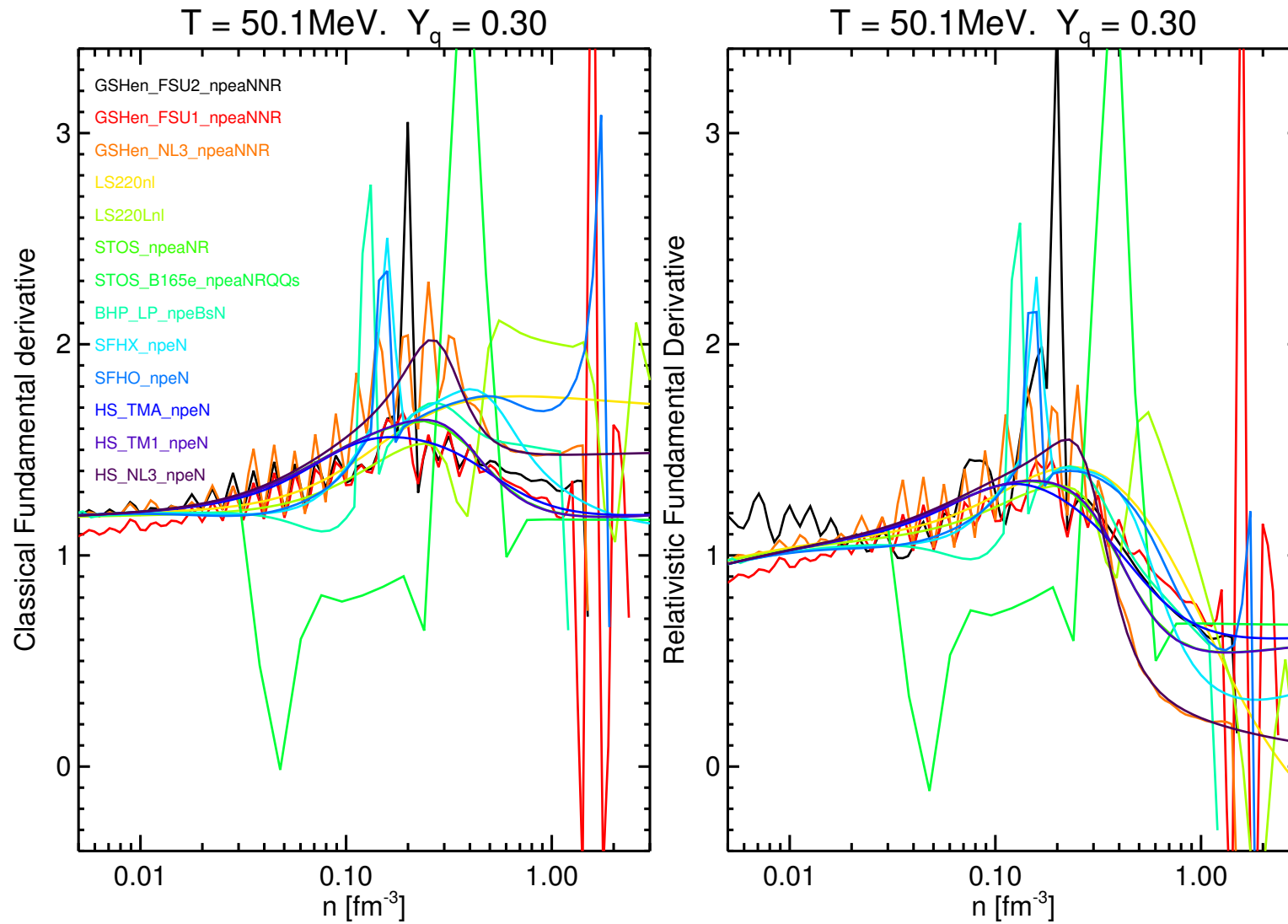
Non-Convexity

In classical fluid dynamics, the convexity of a thermodynamical system is determined by the EOS and, more specifically, by the so-called fundamental derivative (see Isabel's talk):

$$\mathcal{G}_{(\text{cla})} := -\frac{1}{2} V \frac{\frac{\partial^2 p}{\partial V^2} \Big|_s}{\frac{\partial p}{\partial V} \Big|_s}$$

$$\mathcal{G}_{(\text{rel})} = \mathcal{G}_{(\text{cla})} - \frac{3}{2} c_{s(\text{rel})}^2 \cdot$$

Non-Convexity



Motivated by the indications of the existence of possible regions in the dense-matter EOS where the thermodynamics can be non-convex, we performed a numerical study of the structure and dynamics of compact stellar configurations described by a BZT fluid.

For our study we consider the dynamics of unstable and uniformly-rotating neutron stars that collapse gravitationally to black holes.

A phenomenological NC EOS

We choose a particularly simple form of the EOS, namely an ideal gas EOS with an adiabatic index which depends on the density. While this phenomenological EOS can only be regarded as a toy-model, it serves nonetheless to exemplify the particularities that appear when the EOS is non-convex.

The pressure p obeys an ideal-gaslike EOS of the form, GGL-EOS (Gaussian Gamma Law):

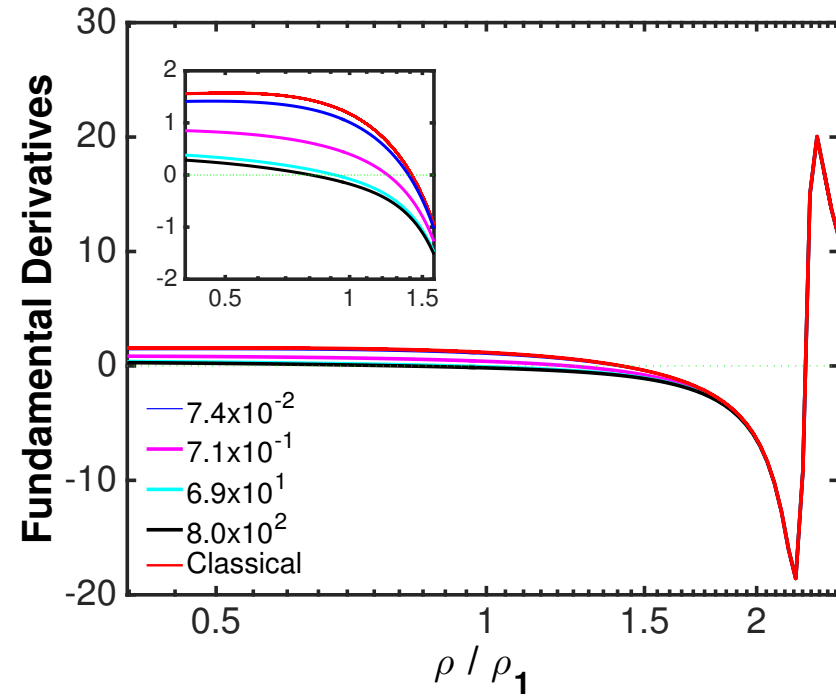
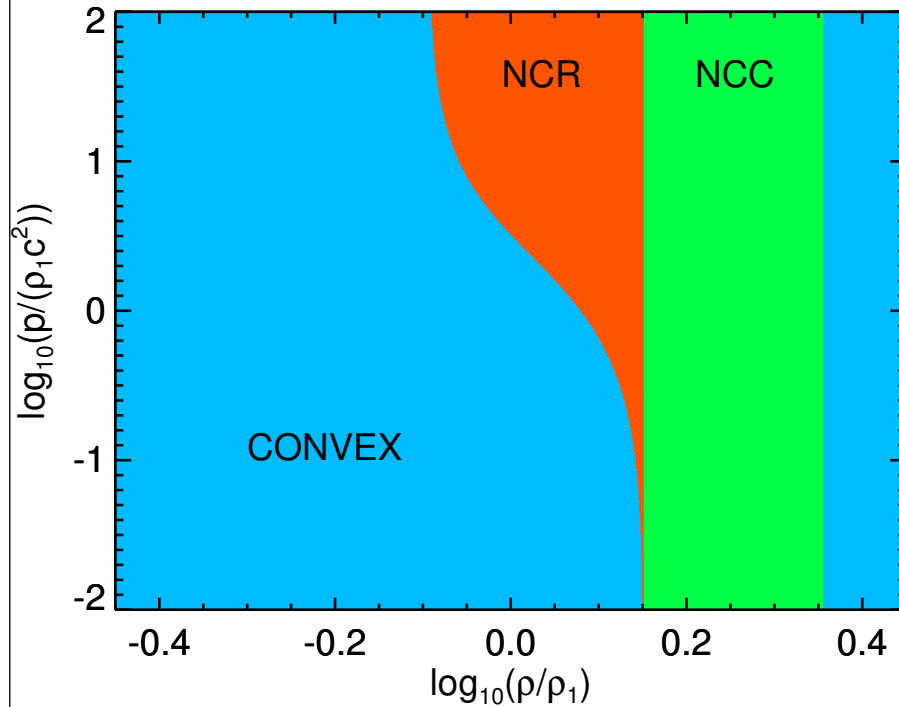
$$p = (\gamma - 1)\rho\epsilon$$

$$\gamma \equiv \gamma_0 + \mathcal{K} \exp\left(-\frac{x^2}{\sigma^2}\right),$$

$$\mathcal{K} := \gamma_1 - \gamma_0, \quad x := \rho - \rho_1$$

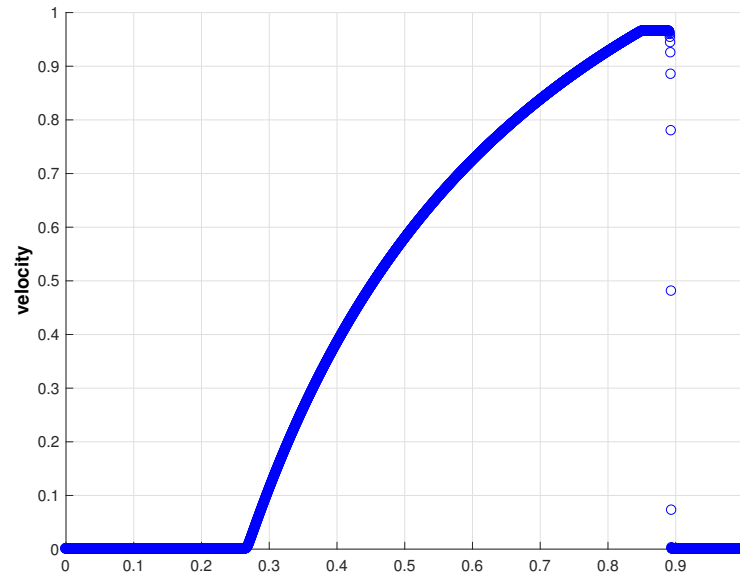
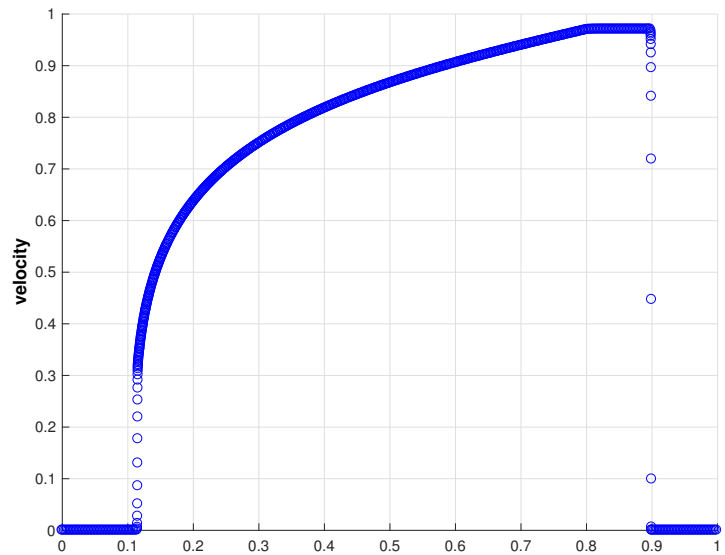
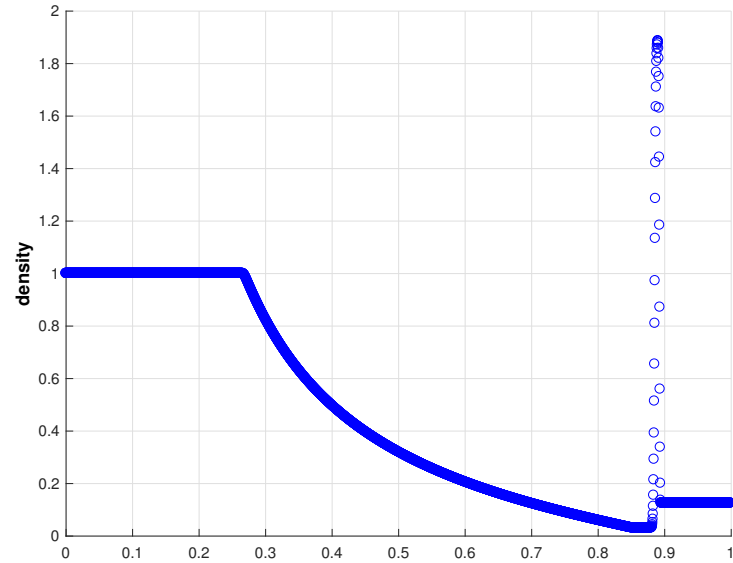
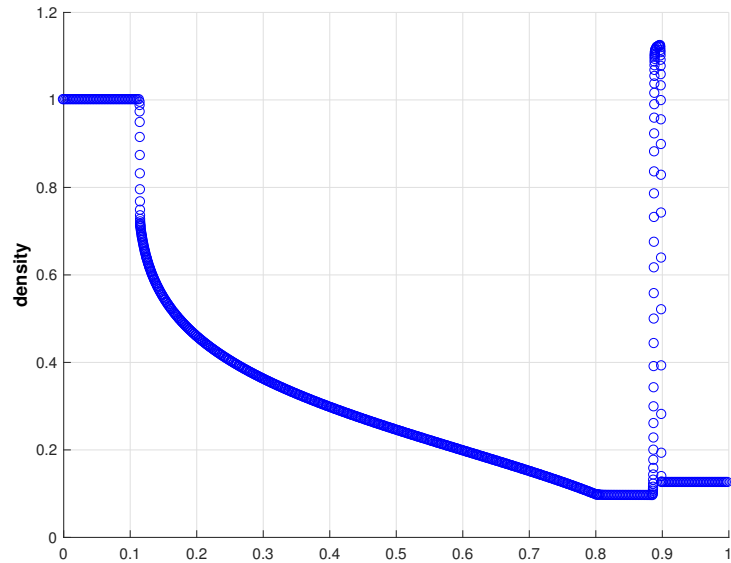
GGL-EOS

$$\gamma_1 = 1.9, \gamma_0 = 4/3, \sigma = 1.1, \rho_1 = 10^{15} \text{ g/cm}^3$$



The FD becomes negative -> **Non convex region!**

Relativistic blast wave test



Gravitational collapse of RNS

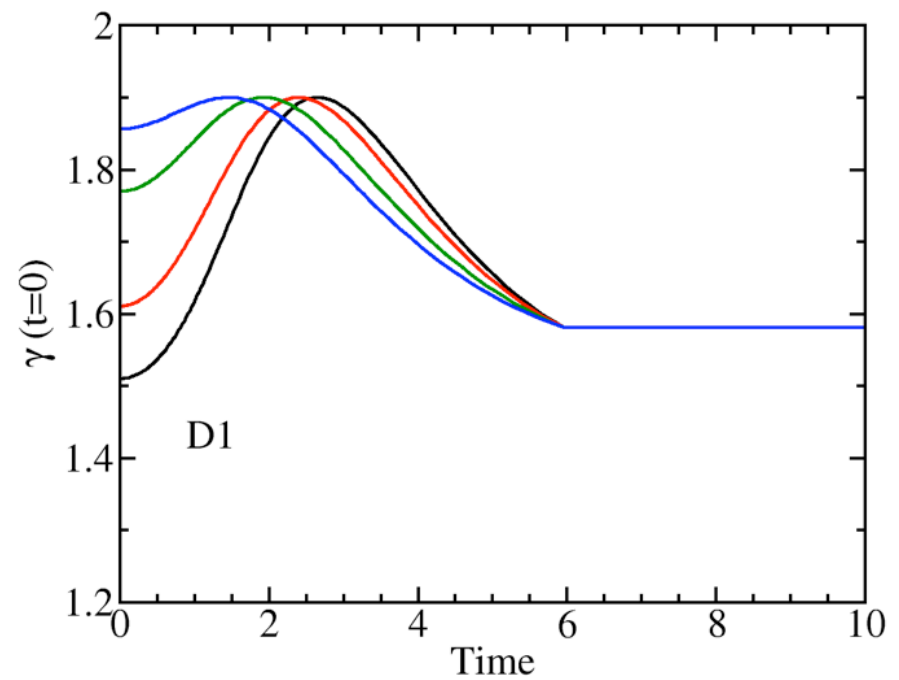
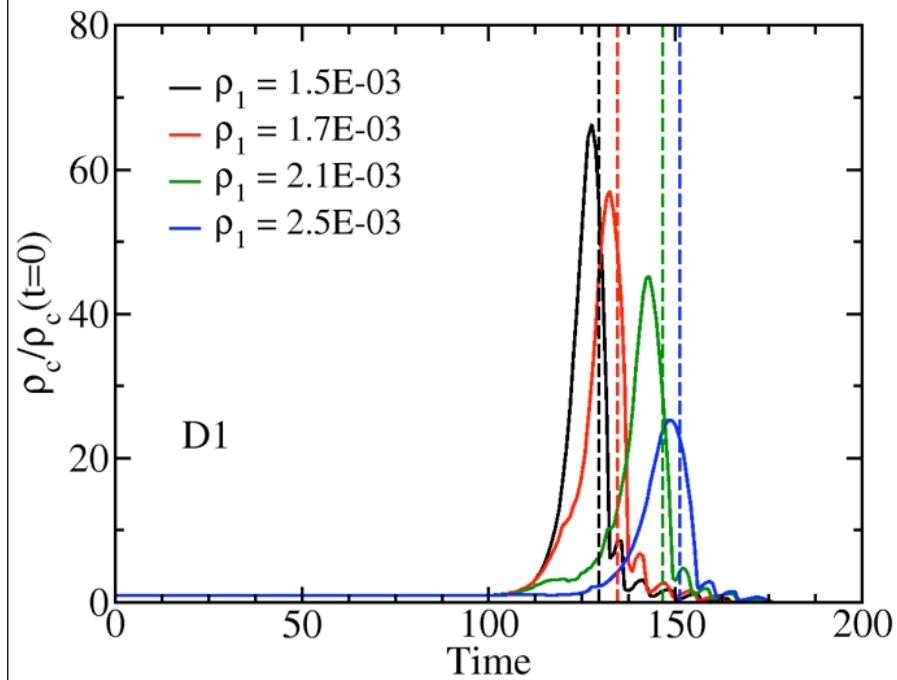
Table 1. Uniformly rotating neutron star models with $\gamma = 2$ and $\kappa = 100$. From left to right the columns report the name of the model, the central density ρ_c in code units and in cgs units, the ratio of polar-to-equatorial coordinate radii r_p/r_e , the gravitational mass M_G , and the circumferential equatorial radius R_e .

Model	ρ_c	ρ_c (g/cm ³)	r_p/r_e	M_G	R_e
D1	3.280×10^{-3}	2.046×10^{15}	0.95	1.665	7.74
D4	3.116×10^{-3}	1.944×10^{15}	0.65	1.861	9.65

Table 2. Parameters of the GGL-EOS used in the rotating neutron star collapse simulations.

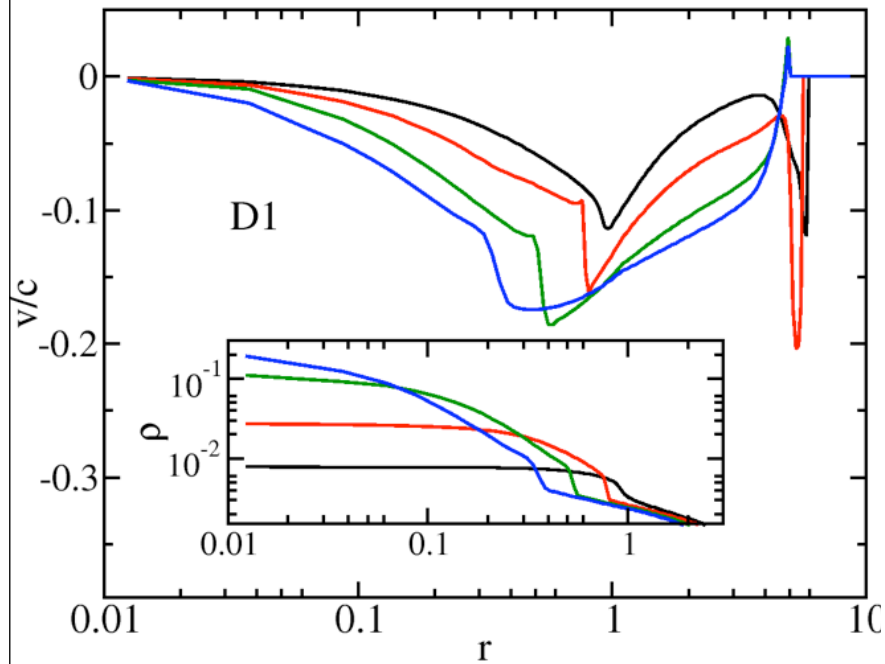
γ_0	γ_1	σ	ρ_1	ρ_1 (g/cm ³)
4/3	1.9	1.10	1.5×10^{-3}	9.356×10^{14}
4/3	1.9	1.10	1.7×10^{-3}	1.060×10^{15}
4/3	1.9	1.10/ 1.15/ 1.20/ 1.50	2.1×10^{-3}	1.310×10^{15}
4/3	1.9	1.10	2.5×10^{-3}	1.559×10^{15}

Gravitational collapse of RNS

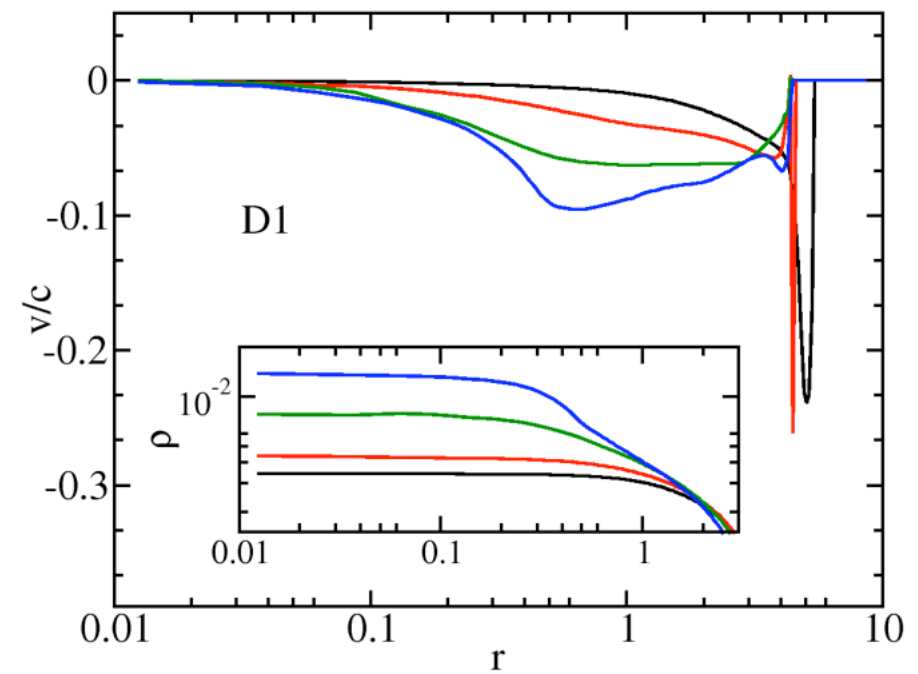


Gravitational collapse of RNS

$$\rho_1 = 1.5E - 3$$

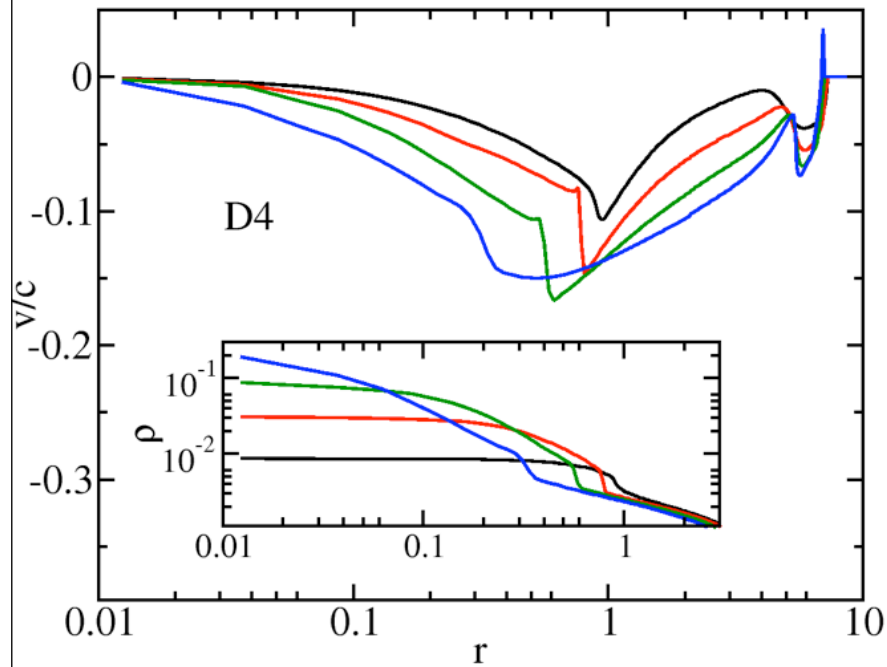


$$\rho_1 = 2.5E - 3$$

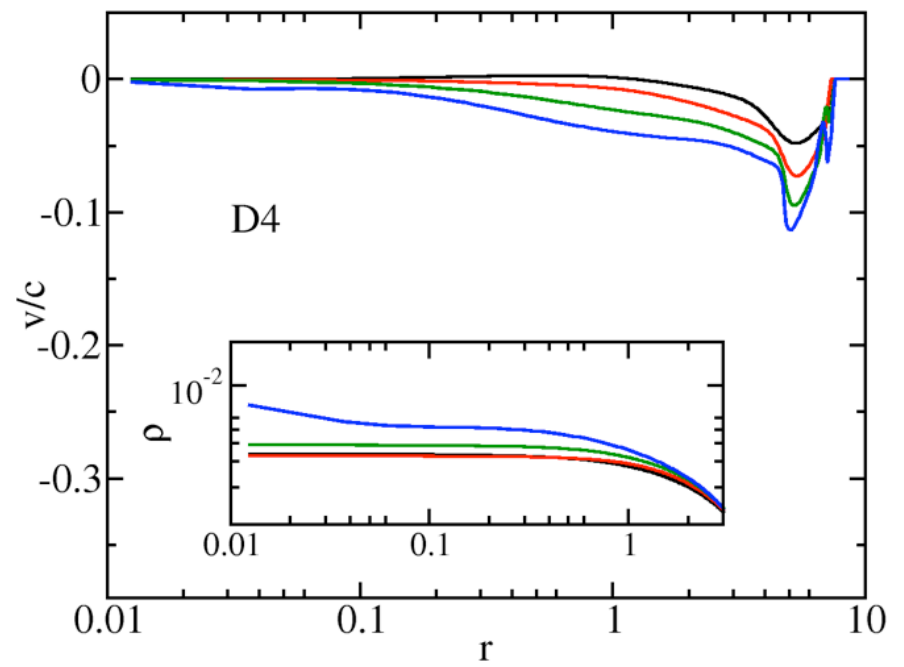


Gravitational collapse of RNS

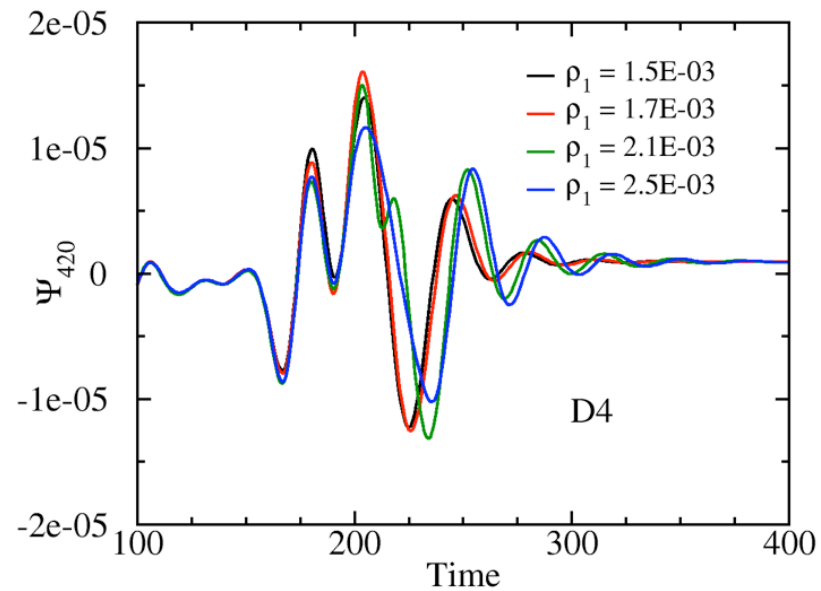
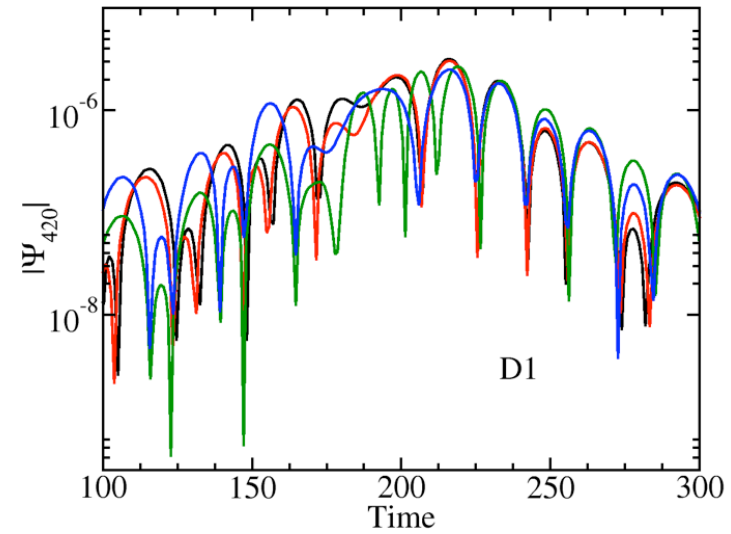
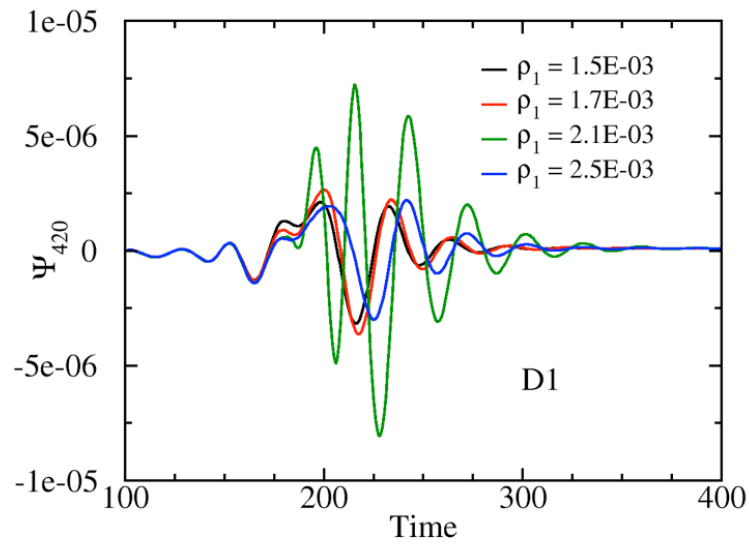
$$\rho_1 = 1.5E - 3$$



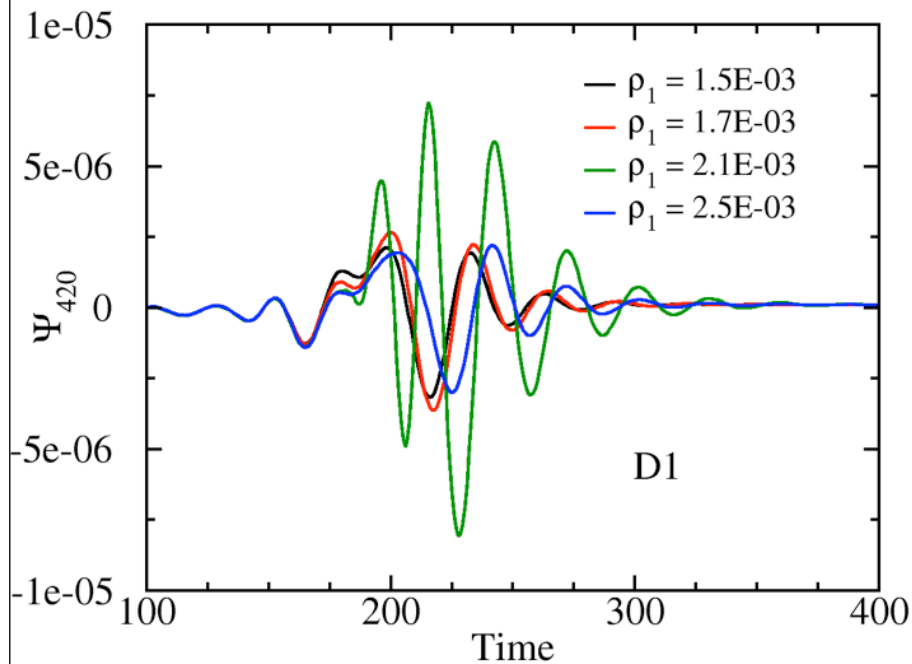
$$\rho_1 = 2.5E - 3$$



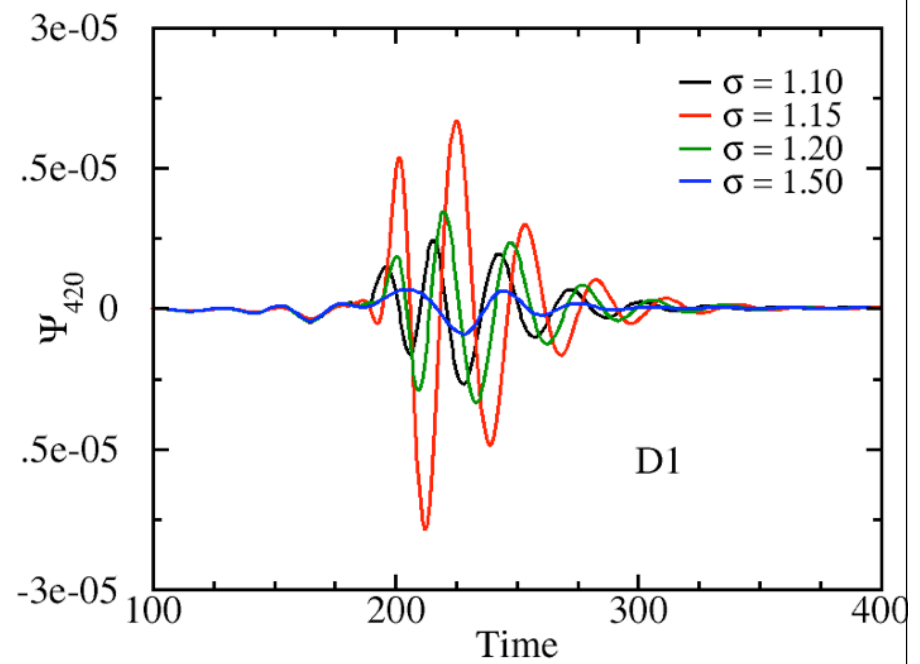
Gravitational wave radiation



Gravitational wave radiation



Fixed width:
 $\sigma = 1.1$



Fixed density parameter:
 $\rho_1 = 2.1E - 3$

Summary

- The EOS of high-density matter might contain regions in which the thermodynamics may be non-convex. The so-called BZT flows are subject to non-convex dynamics and are characterized by the appearance of compound waves (rarefaction shocks) during the evolution.
- We have chosen a simple, phenomenological, non-convex EOS, namely an ideal-gas EOS with an adiabatic index which depends on the density.
- The numerical simulations of collapsing stars have shown the appearance of the characteristic compound waves of BZT fluids and have also illustrated how the non-convex dynamics is also imprinted on the gravitational-wave signals associated with the infalling phase.
- A future study using actual microphysical EOS from nuclear physics will be presented elsewhere.