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Heavy-Ion Collisions (II)

Néstor Armesto Departamento de Física de Partículas and IGFAE, Universidade de Santiago de Compostela nestor.armesto@usc.es

Contents:

- I. Basic ideas about high- p_T particle and heavy flavor production.
- 2. Radiative energy loss.
- 3. DIS on nuclei.
- 4. Linear and non-linear evolution equations: saturation; the CGC.
- 5. Heavy-ion collisions at the LHC.

See Ellis, Stirling, Webber, QCD and Collider Physics, Cambridge, 2003; Casaderrey-Solana, Salgado, arXiv:0712.3443 [hep-ph] and refs. therein; NA, hep-ph/0604108 and refs. therein; Roberts, The structure of the proton, Cambridge; contributions to QCD perspectives on Hot and Dense Matter, Kluwer.

Heavy-Ion Collisions (II).

Factorization:



- Nuclear corrections no medium, QGP or not - to parton densities and fragmentation functions poorly known.
- Nuclear effects usually discussed through the ratio measured/expected: nuclear modification factor, =1 in absence of nuclear effects.
 Heavy-Ion Collisions (II): 1. Basic ideas.



Factorization: I-particle



- x_i : momentum fraction of hadron N (in A) taken by parton i.
- z: momentum fraction of parton i taken by hadron h.
- Scales: Q, μ_F for factorization, μ_R for renormalization.
- f's and D's evolved according to DGLAP.
- DGLAP evolution and partonic σ computed at NLO (order α_s^2 ,...) for all observables of interest (h, H, γ , DY, jets).
- Need of resummation of large logs (e.g. $\log(M_Q/p_T)$).

Heavy-Ion Collisions (II): I. Basic ideas.



Hard probes - theory: 2. Radiative energy loss.



Hard probes - theory: 2. Radiative energy loss.

Medium effects:

• Collinear factorization (for $Q_{E_{cm}} > \Lambda_{QCD}$) is assumed to hold in the medium, with nuclear pdf's evolved using DGLAP and medium-modified fragmentation functions:

$$D_{i \to h}^{med}(x, Q^2) = \int_0^1 \frac{d\epsilon}{1 - \epsilon} P(\epsilon) D_{i \to h}^{vac}\left(\frac{x}{1 - \epsilon}, Q^2\right)$$

• Fragmentation like in vacuum: outside the medium which should be true for large energies (or p_T for $\eta=0$).

• $P(\varepsilon)$: probability to lose some energy (quenching weights) by any kind of energy loss mechanism, either collisional through multiple collisions, or radiative through multiple gluon emission. The latter is suppose to be the dominant phenomenon at large energies.



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Qualitative arguments:



Consider the de-coherence process $|qg\rangle \rightarrow |q\rangle+|g\rangle$ (PI) and define the transport coefficient $qhat=\mu^2/\lambda$.

$$\phi = \frac{k_T^2}{2\omega} \Delta z \sim 1 \Rightarrow \omega, k_T^2 \ll 1 \text{ suppressed} \qquad \phi \sim \frac{\hat{q}L}{2\omega} L = \frac{\omega_c}{\omega} \sim 1 \Rightarrow \omega > \omega_c \text{ suppressed}$$

⇒ IRC safe!!!!

$$\hat{q}t_{coh} \simeq \frac{\hat{q}\omega}{\langle k_T^2 \rangle} \simeq \langle k_T^2 \rangle, \quad \langle k_T^2 \rangle \simeq \sqrt{\hat{q}\omega}$$

$$-\frac{dE}{dz} = \int d\omega \frac{1}{t_{coh}} \omega \left. \frac{dI}{d\omega} \right|_{1 \ scat} \simeq \alpha_s C_R \int^{\omega_c} d\omega \sqrt{\frac{\hat{q}}{\omega}} \Rightarrow -\Delta E \propto \alpha_s C_R \hat{q} L^2$$

Models:

Medium-modified gluon radiation through interference of production and rescattering.



Two parameters define the medium: one characterizing the density and strength of interactions with the medium, plus the length (geometry, dynamical expansion).

Models:



Heavy-Ion Collisions (II): 2. Radiative energy loss.

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Radiative eloss: light hadrons (I)



Heavy-Ion Collisions (II): 2. Radiative energy loss.

Radiative eloss: light hadrons (I)



Heavy-Ion Collisions (II): 2. Radiative energy loss.

Radiative eloss: non-photonic e's

- Prediction from radiative energy loss: $\Delta E(g) > \Delta E(q) > \Delta E(Q)$.
- Non-photonic electrons not conclusive: benchmark, hadronization, collisional, resonances, dynamical medium,...
- Very difficult observable: disentangle
- c, b, heavy mesons,...





Radiative eloss: limitations

• The extracted value of qhat depends on medium model $I < qhat < I 5 GeV^2/fm \Rightarrow$ interface with realistic medium.

 Calculations done in the high-energy approximation: only soft emissions energy-momentum conservation imposed a posteriori ⇒ Monte Carlo.

 Multiple gluon emission: Quenching Weights independent (Poissonian) gluon emission: assumption! ⇒ Monte Carlo (PQM, PYQUEN, YaJEM, JEWEL, Q-PYTHIA).

• No role of virtuality in medium emissions; medium and vacuum treated differently \Rightarrow modified DGLAP evolution.

Radiative eloss: limitations



Monte Carlo (I):



• Assumption: hadronization is not affected by the medium: looks OK at RHIC for p_T >7-10 GeV.

• The splittings are modified: either radiatively (Q-PYTHIA) or radiative+collisionally (JEWELL, PYQUEN); or the evolution is enlarged due to momentum broadening (YaJEM).

• Underlying ingredients: factorization no emission/emission/no emission/... (Sudakov/splitting/Sudakov/...) holds in the medium, and the evolution scale (t,k_T,Θ) can be related with the medium length \rightarrow both to be proved (Jet Calculus in a medium).

Monte Carlo (II):

- The MC's generically reproduce the expectations:
 - → Particle spectrum softens (jet quenching).
 - → Emission angle enlarges (jet broadening).
 - → Intra-jet multiplicity enlarges.

Monte Carlo (II):





• Intense activity at RHIC and the LHC: jet reconstruction in a large background (small clustering parameters versus out-of-'cone' medium modification).



Jets (I):

• Single-particle inclusive distributions suffer from several biases: steep partonic spectrum which enhances small energy losses (trigger bias), geometric bias towards the surface,...

• They come from our inability to reconstruct the energy of the 'parton': we cannot distinguish a low energy, little degraded one from a high energy, highly degraded one.

Jets are the most direct of all hard probes of the medium.

As close as you can get to the original quark or gluon near its time of creation



Jets come
 with a
 definition:
 clustering or
 reconstruction
 algorithm.

Jets (I):



Jets (II):

• Techniques for background substraction (the underlying event), designed to deal with the pileup at the LHC, can be applied in HI.

• Note: typically several 100 GeV are deposited per unit in $\eta \times \Phi$.



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DIS on nuclei:

$$R_{F_2}^A(x, Q^2) = \frac{F_2^A(x, Q^2)}{AF_2^{\text{nucleon}}(x, Q^2)}$$

- R=I indicates the absence of nuclear effects.
- R≠I discovered in the early 70's.
- Each region demands a different explanation.
- I will be mostly interested in small x (<0.1) relevant for high energies: isospin effects neglected.
- Heavy-Ion Collisions (II): 3. DIS on nuclei.



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DIS on nuclei:



Global fits:

→ Data in EPS09 (Q², M²>1.69 GeV²; p_T >1.7 GeV): 92 from DY (E-772 and 886), 20 from π^0 (PHENIX), rest up to 929 from DIS (E-135, EMC, NMC). Neutrino data under discussion.

Cross sections computed in collinear factorization

$$\Rightarrow$$
 Define $R_i^A(x,Q^2) = rac{f_i^A(x,Q^2)}{f_i^p(x,Q^2)}$

Using a known set for free protons (CTEQ, MRST....)

and DGLAP evolution of the nuclear and free proton PDFs

 \Rightarrow Find the minimum of χ^2



Heavy-Ion Collisions (II): 3. DIS on nuclei.

Global fits:

- → Eskola '94: DGLAP for nuclei.
- → EKS98: first global analysis, LO, DIS+DY.
- → Others non global analysis: Indumathi-Zhu, FGS.
- \rightarrow nDS (2003): 1 st NLO, DIS.
- \rightarrow HKM, HKN (2001-07): NLO, χ^2 minimization, DIS+DY.
- → EKPS07: LO, error analysis, 1st look at RHIC data.
- → EPS08: LO, BRAHMS forward data (factorization check).
- \rightarrow EPS09: NLO, χ^2 minimization, error analysis.

Heavy-Ion Collisions (II): 3. DIS on nuclei.

Global fits:

→ Eskola '94: DGLAP for nuclei.



Heavy-Ion Collisions (II): 3. DIS on nuclei.

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DGLAP/BFKL: $x_{n-1}, k_{T,n-1}, x_{n-2}, k_{T,n-2}$ x_{n}, Q_n x_{n}, Q_n $dP_i = \frac{dx_i}{x_i} \frac{dk_{T,i}^2}{k_{T,i}^2}, \quad \omega_i = x_i E, \quad \theta_i^2 \simeq \frac{k_{T,i}^2}{\omega_i^2} \quad x_n \ll x_{n-1} \ll x_{n-2} \ll \dots \ll x_1 \ll x_0$

A) DGLAP (DLA): $Q_n^2 \gg k_{T,n-1}^2 \gg k_{T,n-2}^2 \gg \ldots \gg k_{T,1}^2 \gg Q_0^2$

$$\int_{Q_0}^{Q_n} dP_{n-1} \int_{Q_0}^{k_{T,n-1}} dP_{n-2} \dots \int_{Q_0}^{k_{T,2}} dP_1 \propto \left[\frac{\alpha_s N_c}{\pi} \ln \frac{Q_n}{Q_0}\right]^n$$

B) BFKL:
$$\int_{x_n}^{x_0} dP_{n-1} \int_{x_{n-1}}^{x_0} dP_{n-2} \dots \int_{x_2}^{x_0} dP_1 \propto \left[\frac{\alpha_s N_c}{\pi} \ln \frac{x_0}{x_n}\right]^n$$

• Both of them lead to a gluon distribution at small x behaving like $xg(x,Q^2) \propto x^{-\lambda}$ at fixed Q^2 , $\lambda \approx 0.2$ -0.3 in data.





• Unitarity (probability conservation in QM) implies that the (Img forward) scattering amplitude N \leq I (optical theorem $\Rightarrow \sigma_{\propto}$ N). But $xg(x,Q^2) \propto \int^{Q^2} dk^2 \phi(x,k^2), \ \phi(x,k^2) \propto \int \frac{d^2r}{r^2} e^{ik \cdot r} N(x,r)$

so $xg(x,Q^2) \propto x^{-\lambda}$ at fixed Q^2 is not compatible with unitarity. The most celebrated dipole model is GBW, $Q_s^2 \propto x^{-\lambda}$.

$$\mathcal{N}^{GBW}(r, Y = 0) = 1 - \exp\left[-\left(\frac{r^2 Q_{s0}^2}{4}\right)^{\gamma}\right]$$

Unitarity:



The 'phase' diagram:



collisions.

al, McLerran-Venugopalan.
Arguments:

• At small enough x for the projectile to interact coherently with the whole hadron, the CGC offers a description of the $x \leq \frac{1}{2m_N R_A} \sim 0.1 A^{-1/3}$ hadron wave function.

• The RG equation for the slow/fast separation (JIMVVLK) was derived for scattering of a dilute projectile on a dense



target. Gluon # becomes as high as it can (α_s^{-1}) be below Q_s^2 .

• Its mean-field version (the Balitsky-Kovchegov equation, P2) is used for phenomenology: numerically and analytically understood. *Heavy-lon Collisions (II): 4. Saturation.*



Heavy-Ion Collisions (II): 4. Saturation.

• Geometric scaling also found in eA.

$$\frac{\sigma^{\gamma^* A}(\tau_A)}{\pi R_A^2} = \frac{\sigma^{\gamma^* p}(\tau_A)}{\pi R_p^2}$$
$$\frac{Q_{s,A}^2}{Q_{s,p}^2} = \left(\frac{A\pi R_p^2}{\pi R_A^2}\right)^{\frac{1}{\delta}} \Rightarrow \frac{\tau_A}{\tau_p} = \left(\frac{\pi R_A^2}{A\pi R_p^2}\right)^{\frac{1}{\delta}}$$
$$\delta = 0.79 \pm 0.02 \ (x < 0.02).$$

$$\frac{10}{10} = \frac{10}{10^2} = \frac{$$

NA et al '04



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(qn) مەلەر

0.8

0.6 10

-2

 10^{-1}

pA at RHIC:

• Control experiment for initial state effects in AA: Cronin effect in dAu at midrapidity ruled out initial state effects as the explanation for the suppression observed in AA.

• Suppression at forward rapidities was predicted by small-x evolution (BK).









$$R_{dAu} \to_{y \to \infty} A^{-(1-\gamma/\delta)/3}(fc)$$
$$A^{-1/3}(rc, fluctuations)$$

AA at RHIC:



• Now it has been done with the available NLO-BK machinery.



Geometric scaling
 is enough:
 factorization of
 geometry and energy
 dependences.

Heavy-Ion Collisions (II): 4. Saturation.

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Present status:

Observable at RHIC	Standard interpretation
Low multiplicity (~2/3 expectations	Strong coherence in particle production:
dN _{ch} /dη _{η=0} ~1000 for central	CGC, collectivity, strong gluon
collisions)	shadowing!?
v2 in agreement with ideal hydro	Almost ideal fluid, very fast thermalization/
(η/s~a few/(4π))	isotropization, strongly/weakly coupled!?
Strong jet quenching (R _{AA} (10 GeV)	Opaque partonic medium, radiative
~0.2 for π ⁰ , disappearance of back-	(+elastic) energy loss, weak/strong
to-back correlations)	interaction with the medium!?

All these observation have triggered new theoretical developments (e.g. how to treat a strongly coupled system - AdS/CFT) to:

- Check our theoretical explanations of the probes.
- Constrain our understanding of medium properties.

Heavy-Ion Collisions (II): The picture from RHIC.

Open problems:

• Highlight: the medium created in the collisions is dense, ~10 GeV/ fm³, partonic and behaves very early like a quasi-ideal fluid; strong collectivity: scQGP. New theoretical developments:

A) Why the medium gets thermalized so early (T<I fm)? Instabilities, perturbative HO processes, strong coupling phenomena (studied in N=4 SYM using the AdS/CFT correspondence), CGC.

B) The value of qhat is? too large for pQCD: strong coupling?

C) Why the viscosity is so low? How to do viscous hydro?

D) Differential observables; and jet-medium interactions?

Heavy-Ion Collisions (II): The picture from RHIC.

HICOLHC:

• LHC started accelerating ion beams on 04.11.2010: 2.76 ATeV.

 Ist collisions on 07.11.2010; now ~ 10⁸ recorded events in ALICE+ATLAS+CMS.



- First paper on arXiv on 17.11.2010:ALICE, multiplicities in central collisions, arXiv:1011.3916 [nucl-ex].
- 12 papers until now:

* ALICE: 6 (2 on multiplicities, 2 on flow, 1 on jet quenching, 1 on interferometry).

* ATLAS: 2 (1 on jets, 1 on J/ ψ and Z).

* CMS: 4 (I on jets, I, on W/Z, I on correlations, I on quarkonia). + many new results in QM2011(<u>http://qm2011.in2p3.fr</u>/). Heavy-lon Collisions (II): 5. LHC.



A Large Ion Collider Experiment







A Large Ion Collider Experiment





Heavy-Ion Collisions (II): 5. LHC.

ALICE data on multiplicities:



ALICE data on centrality:



Azimuthal asymmetries:



Azimuthal asymmetries:



Azimuthal asymmetries:



Heavy-Ion Collisions (II): 5. LHC.

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Results for RAA:



Results for RAA:



LHC-specific: dijets





LHC-specific: dijets



Dijets (II):



 Small kick to the gluons which go 'out-of-cone' may lead to this additional jet-energy 'degradation'.

- $E_{gluon} < \sqrt{qhatL}$ gives qhatL=50-100 GeV², in rough agreement with RHIC extrapolations.
- In pp there is already a lot of degradation (<x> differs ~ 10 %).

Heavy-Ion Collisions (II): 5. LHC.

Casalderrey-Solana, Milhano, Wiedemann, 1012.0745; also Qin and Müller, 1012.5280



Dijets (II):



Quarkonia:



$$\begin{split} \Upsilon(2S+3S)/\Upsilon(1S)\Big|_{pp} &= 0.78^{+0.16}_{-0.14} \pm 0.02 \qquad \Upsilon(2S+3S)/\Upsilon(1S)\Big|_{PbPb} = 0.24^{+0.13}_{-0.12} \pm 0.02 \\ &\frac{\Upsilon(2S+3S)/\Upsilon(1S)\Big|_{PbPb}}{\Upsilon(2S+3S)/\Upsilon(1S)\Big|_{pp}} = 0.31^{+0.19}_{-0.15} \pm 0.03 \end{split}$$

- J/ ψ results do not show enhancement.
- Higher BBbar states show larger suppression (CMS): termometer?



Rapidity correlations (I):



Rapidity correlations (II):



PbPb@2.76 TeV/n

• Long range rapidity correlations in particle production appear naturally in several models: string models with a varying number of them, CGC,...

• Origin of the elongation in η for the ridge unsettled yet: coupling fragmentation \leftrightarrow flowing medium, ISR, flow itself (v₃),...

Summary:

Observable at RHIC	Standard interpretation	Prediction for the LHC
Low multiplicity	Strong coherence in particle production	dN _{ch} /dη _{η=0} <1700 for central collisions √
v2 in agreement with ideal hydro	Almost ideal fluid	Similar or smaller $v_2(p_T)$
Strong jet quenching	Opaque medium	R _{AA} (20 GeV)~0.1-0.2 for π ⁰

• Quite a bit for less than 7 weeks of data taking!!!

• The very first data seem, at first sight, not to be in dispute with the claims at RHIC - the problems remain too.

• LHC offers new opportunities, both enlarging the lever arm (in energy, in p_T ,...) for existing observables and offering new ones (identified heavy quarks, jets, correlations,...). Fun has just begun!!!

Summary:

Plans (tentative!?):

* PbPb @ 2.76 ATeV: four weeks at the end of 2011; at least 3 times the luminosity in 2010. End of 2012?
* pPb @ 4.4 ATeV: studies during the PbPb run in 2011, run at the end of 2012?

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- Heavy-Ion Collisions (II): 5. LHC.



Heavy-Ion Physics (II).

Model list:



Heavy-Ion Collisions (II): Backup.

Embedding in a medium:

• Calculation of eloss has to be embedded in a geometry:

* Homogeneous piece of fixed length \Rightarrow qhat~I GeV²/fm.

* Density diluting as $I/T \Rightarrow$ qhat~I GeV²/fm. * Medium as overlap (N_{coll}), T_A(s)T_B(b-s) \Rightarrow qhat~I0 GeV²/fm.

* Hydrodynamical medium $\Rightarrow \kappa \sim 2-4$.

$$\hat{q}(\xi) = K\hat{q}_{\text{QGP}} \simeq K \cdot 2e^{3/4}(\xi)$$

Note: production points sampled as N_{coll or} N_{part}. Heavy-Ion Collisions (II): Backup.





Radiative eloss: light hadrons (II)



Radiative eloss: light hadrons (II)



Radiative eloss: limitations

• The extracted value of qhat depends on medium model $I < qhat < I 5 GeV^2/fm \Rightarrow$ interface with realistic medium.

 Calculations done in the high-energy approximation: only soft emissions energy-momentum conservation imposed a posteriori ⇒ Monte Carlo.

 Multiple gluon emission: Quenching Weights independent (Poissonian) gluon emission: assumption! ⇒ Monte Carlo (PQM, PYQUEN, YaJEM, JEWEL, Q-PYTHIA).

• No role of virtuality in medium emissions; medium and vacuum treated differently \Rightarrow modified DGLAP evolution.

Radiative eloss: limitations

• The extracted value of qhat depends on medium model $I < qhat < I 5 GeV^2/fm \Rightarrow$ interface with realistic medium.

• Calculat $\omega \frac{dI}{d\omega} = \int_0^{k_T^{2,max}} dk_T^2 \,\omega \frac{dI}{d\omega dk_T^2}, \quad \Delta E = \int_0^E d\omega \,\omega \frac{dI}{d\omega} \qquad \text{ily soft}$ emissions \Rightarrow

Monte Ca $P(\Delta E) = \omega \frac{dI}{d\omega} = \int_0^{k_T^{2,max}} dk_T^2 \,\omega \frac{dI}{d\omega dk_T^2}, \quad \Delta E = \int_0^E d\omega \,\omega \frac{dI}{d\omega}$

• Multip'-(Poisson $P(\Delta E) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[\prod_{i=1}^{n} \int d\omega_i \frac{dI(\omega_i)}{d\omega} \right] \delta \left(\Delta E - \sum_{i=1}^{n} \omega_i \right) \exp \left[- \int d\omega \frac{dI}{d\omega} \right]^2 QM,$ PYQU⁻

 $P_{trunc}(\Delta E) = p_0 \delta(\Delta E) + P_{cont}(\Delta E)\Theta(E - \Delta E) + \delta(E - \Delta E) \int_E^\infty d\epsilon P(\epsilon)$

• No lote of meaning in meaning emissions, meaning and vacuum treated differently \Rightarrow modified DGLAP evolution.



$$F_2^A(x, Q^2) = \frac{Q^2(1-x)}{4\pi^2 \alpha_{\text{EM}}} \sigma_{\gamma^{*-A}}$$

 Q^2 is the transverse resolution.

x is the momentum fraction (IMF).

 $F_2(x, Q^2) = \sum e_q^2 xq(x, Q^2) \text{ at LO.}$

$l(k) + A(Ap) \longrightarrow$	$\rightarrow l(k') + X(Ap'),$	$Q^2 = -q^2 >$
q = k - k',	$W^2 = (q+p)^2,$	$x = \frac{-q^2}{2p \cdot q}$

$$\begin{split} Q^2 &= -q^2 > 0 \\ x &= \frac{-q^2}{2p \cdot q} = \frac{-q^2}{W^2 - q^2 - m_{\rm nucleon}^2}, \end{split}$$

- $F_{2(1)}(x, Q^2) = F_{2(1)}(x)$ at large Q²: Bjorken scaling, point-like partons.
- $F_2(x)=2xF_1(x)$: Callan-Gross relation, spin 1/2 quarks.
- I will be interested in small x i.e. large energies W.



$$Q^{2}\partial_{Q^{2}}\begin{pmatrix}q_{i}(x,Q^{2})\\\bar{q}_{i}(x,Q^{2})\\g(x,Q^{2})\end{pmatrix} = \frac{\alpha_{s}(Q^{2})}{2\pi} \int_{x}^{1} \frac{d\xi}{\xi} \begin{pmatrix}P_{q_{i}q_{j}}\begin{pmatrix}\underline{x}\\\xi\end{pmatrix} & 0 & P_{q_{i}g}\begin{pmatrix}\underline{x}\\\xi\end{pmatrix} & P_{q_{i}g}\begin{pmatrix}\underline{x}\\\xi\end{pmatrix}\\P_{gq}\begin{pmatrix}\underline{x}\\\xi\end{pmatrix} & P_{gg}\begin{pmatrix}\underline{x}\\\xi\end{pmatrix} & P_{gg}\begin{pmatrix}\underline{x}\\\xi\end{pmatrix}\end{pmatrix} \begin{pmatrix}q_{j}(x,Q^{2})\\\bar{q}_{j}(x,Q^{2})\\g(x,Q^{2})\end{pmatrix}$$
DGLAP:



Data on the proton:



required for the LHC. Heavy-lon Collisions (II): Backup.

10⁵

 $Q^2(GeV^2)$

10²

10

10³

104

Data on the proton:



- \rightarrow All experimental data where you rely on collinear factorization.
- → Several groups: MSTW, CTEQ, NNPDF, ZEUS, HI, Alekhin.
- → Error analysis using variants of the Hessian method.
- \rightarrow Analysis at LO, NLO and even NNLO (MSTW).
- → Initial conditions for several pdf's: CTEQ, MSTW [$f_i(x,Q_0^2)=A_ix^{bi}$ (1-x)^{ci]},...As many restrictions as possible (e.g. ubar=,≠dbar): around 40 parameters in MSTW and CTEQ (ZEUS, H1 smaller number).

NNPDF: around 400 parameters.



Heavy-Ion Collisions (II): Backup.



Sea decomposition at small x difficult.

Heavy-Ion Collisions (II): Backup.



Heavy-Ion Collisions (II): Backup.

Two scattering case (PI):



$$c(p_+, p'_+)i\mathcal{T}_1(q) = it_{\text{forw}}c(p_+, p'_+)A \int d^2x_T T_A(x_T) e^{-ix_T \cdot (p'_T - p_T)} \implies \sigma_A^1 = A\sigma$$

$$\begin{split} c(p_{+}, p_{+}')iT_{2}(q) &= c(p_{+}, p_{+}')A(A-1)(it_{\text{forw}})^{2} \\ &\times \int \frac{d^{2}k_{T}}{(2\pi)^{2}} dx_{1+} dx_{2+} d^{2}x_{1T} d^{2}x_{2T} \exp\left(-ik_{T}^{2}(x_{2+}-x_{1+})/(2p_{+})\right) \\ &\times \exp(-i[x_{1T} \cdot (k_{T}-p_{T})+x_{2T} \cdot (p_{T}'-k_{T})]\rho_{A}(x_{1+}, x_{1T}) \\ &\times \rho_{A}(x_{2+}, x_{2T})\theta(x_{2+}-x_{1+}), \end{split}$$

Two scattering case (PI):



$$c(p_+, p'_+)i\mathcal{T}_1(q) = it_{\text{forw}}c(p_+, p'_+)A\int d^2x_T T_A(x_T) e^{-ix_T \cdot (p'_T - p_T)} \implies \sigma_A^1 = A\sigma$$

$$\begin{split} c(p_{+}, p_{+}')iT_{2}(q) &= c(p_{+}, p_{+}')A(A-1)(it_{\text{forw}})^{2} \\ &\times \int \frac{\mathrm{d}^{2}k_{T}}{(2\pi)^{2}} \,\mathrm{d}x_{1+} \,\mathrm{d}x_{2+} \,\mathrm{d}^{2}x_{1T} \,\mathrm{d}^{2}x_{2T} \exp\left(-ik_{T}^{2}(x_{2+}-x_{1+})\big/(2p_{+})\right) \\ &\times \exp(-i[x_{1T} \cdot (k_{T}-p_{T})+x_{2T} \cdot (p_{T}'-k_{T})]\rho_{A}(x_{1+},x_{1T}) \\ &\times \rho_{A}(x_{2+},x_{2T})\theta(x_{2+}-x_{1+}), \end{split}$$

Coherence length, shadowing (PI): $\exp\left[-ik_T^2(x_{2+}-x_{1+})/(2p_+)\right] = \exp\left[-i(x_{2+}-x_{1+})/l_c\right], \text{ with } l_c = 2p_+/k_T^2$ A) $p_+ \to 0$ $i\mathcal{T}_2(q) \to 0$ B) $p_+ \to \infty$, exp $[-i(x_{2+} - x_{1+})/l_c] \to 1$ $i\mathcal{T}_2(q) = \frac{A(A-1)}{2} (it_{\text{forw}})^2 \int d^2 x_T \, e^{-ix_T \cdot (p_T' - p_T)} T_A^2(x_T),$ $\sigma_A^2 = \frac{\checkmark}{2} \frac{A(A-1)}{2} \int d^2 x_T [T_A(x_T)\sigma]^2$ The lifetime of the qqbar fluctuation is $\geq R_A$ for $x \leq 0.1 A^{-1/3}$. $|_{c}$ $\tau \sim \frac{1}{Q} \times \frac{E_{\text{lab}}}{Q} \simeq \frac{W^2}{2m_{\text{nucleon}}Q^2} \simeq \frac{1}{2m_{\text{nucleon}}x}$

$$\chi^2 \approx \chi_0^2 + \sum_{ij} \delta a_i H_{ij} \delta a_j \quad H_{ij} \equiv \frac{1}{2} \frac{\partial^2 \chi^2}{\partial a_i \partial a_j} \Big|_{a=a^0} \quad \chi^2 \approx \chi_0^2 + \sum_i z_i^2$$

$$\Delta \chi^{2} \equiv \sum_{i} \frac{\Delta \chi^{2}(z_{i}^{+}) + \Delta \chi^{2}(z_{i}^{-})}{2N} \approx \sum_{i} \frac{(z_{i}^{+})^{2} + (z_{i}^{-})^{2}}{2N}, \quad S_{1}^{\pm} = \pm \delta z_{1}^{\pm} (1, 0, 0, \dots, 0)$$
$$S_{2}^{\pm} = \pm \delta z_{2}^{\pm} (0, 1, 0, \dots, 0)$$

$$(\Delta X)_{\text{extremum}}^2 \approx \Delta \chi^2 \sum_j \left(\frac{\partial X}{\partial z_j}\right)^2 \qquad (\Delta X^-)^2 \approx \sum_k \left[\max\left\{X(S_k^+) - X(S^0), X(S_k^-) - X(S^0), 0\right\}\right]^2$$
$$(\Delta X^-)^2 \approx \sum_k \left[\max\left\{X(S^0) - X(S_k^+), X(S^0) - X(S_k^-), 0\right\}\right]^2$$

Note: any error analysis is linked to a functional form for the i.c. (NNPDF implies more flexibility); pdf's errors to be used, too. *Heavy-lon Collisions (II): Backup.*

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The BK equation:



pA at RHIC:

 $l^3 N / (dy_h d^2 p_t) [(GeV)^{-1}]$

1×10

• This suppression is compatible with ugd+factorization (dilutedense): IIM, DHJ, in agreement with ep + $A^{1/3}$ prescription for Q_s^2 . It is also compatible with the ratio of geometric ep/eA scaling functions.



• Warning: $< x_A > > 0.02$, and such suppression also happens at SPS/FNAL energies: finite energy corrections, eloss?



pA at RHIC:

25<E_<30 GeV

S=0.093±0.040

30<E_<55 GeV

2.5

0

 φ_{LCP}

0.2

φ,

 Azimuthal correlations may also indicate small-x dynamics: tale of the two-particle inclusive distributions

(Baier et al, Kovchegov et al, Marquet).

$$\frac{d\sigma}{dy_1 \, dy_2 \, d^2 p_1 \, d^2 p_2 \, d\Delta \phi}$$



0.3**Azimuthal Correlations** Coincidence Probability (radian⁻¹ 0.275 W = 200 GeV $\eta_1 = 3.8, \eta_2 = 0$, central 0.25 $p_1 = 1.5 \text{ GeV}, p_2 = 0.2 - 1.5 \text{ GeV}$ 0.225 25<E_<30 GeV Proton - Proton 0.2 2.5 5 Deuteron - Gold S=0.154±0.024 0.175 0.15 0.125 Kharzeev-Levin-McLerran 30<E_<55 GeV 0.1 ō 3 π

 Charm production described (also Kharzeev et al, Tuchin).

AA at RHIC:







Initial conditions for hydrodynamical evolution are a key ingredient in those calculations. CGC gives larger eccentricity: room for viscosity or larger equilibration times.
Uncertainties at the nuclear periphery (NP region).

AA at RHIC:

• CGC may offer initial conditions for QGP formation: transverse fields transform into longitudinal (Glasma) (Lappi et al. Romatschke et al).



• QCD basis for good old string models.

Figure 4: Glasma flux tubes. The transverse size of the flux tubes is of order $1/Q_s$.



$$\langle n_B \rangle_F = a + b n_F, \quad b \equiv D_{FB}^2 / D_{FF}^2,$$

 $b = \frac{1}{1 + c \alpha^2}$.

• Correlations in rapidity are a place to look for such origin of particle production (Capella et al, NA et al, Dumitru et al, Fukushima et al).

Multiplicities:



W/Z (LHC-specific):



LHC and beyond:





LHC and beyond:



LHC and beyond:

