

Lattice actions

- Derive the plaquette lattice action for the gauge field.
- Prove integration formulas for Grassmann variables.
- Derive the Wilson fermion propagator formula.
- Show that staggered fermions describe four degenerate fermion flavours.

Improved lattice actions

- Show that the twist can be transformed from the Wilson term to the mass term and vice versa.
- Prove the chiral WT-identities in tmLQCD.
- Derive the chiral states of domain wall fermions.
- Prove the GW-relation for Neuberger fermions.

Monte Carlo integration

- Prove that the Metropolis algorithm satisfies detailed balance.
- Show that $\min(1, R)$ in the Metropolis algorithm can be replaced by $R/(1+R)$.
- Derive the recurrence relations for the exponential function of $SU(3)$ matrices.
- Prove that detailed balance is satisfied by the noisy correction in PHMC.

Error estimates

- Prove the formula for variance in terms of the integrated autocorrelation.
- Show that the jackknife analysis gives the correct errors.